

L 54932-65  
ACCESSION NR: AP5019226

mechanism is suggested according to which NaCl, which initially is a dielectric, is turned by the shock wave front into a semiconducting state with donor levels. The concentration of the donors generated by the shock wave front during plastic deformation reaches  $10^{-3}$ . Free carriers in the conduction band are generated as a result of thermal excitation of electrons from the donor levels. Orig. art. has:

13 formulas and 3 figures.

[65]

ASSOCIATION: none

ITEM NUMBER: 65

ENCL: 00

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NO REF Sov: 014

OTHER: 020

ATT PRESS: 4051

Card 2/2

KOLMEROVA,Czeslawa; KRAUSE,Mieczyslaw

Cathode follower and its use in physiology. Acta physiol. polon. 11  
no,2:341-344 Mr-Ap '60.

1. Z Zakladu Elektroniki Przemyslowej Politechniki Slaskiej w  
Gliwicach, Kierownik: prof. dr inż. T. Zagajewski; i z Zakladu  
Fizjologii Slaskiej A. M. v Zabrsu-Rokitnicy, p.o. Kierownika:  
dr M. Krause.

(ELECTROPHYSIOLOGY equip. & suppl.)

KOLMEROWA, C.; WASOWICZ, B.

Electric-resistance strain gauges. p. 6.

POMIARY, AUTOMATYKA, KONTROLA. (Naczelnna Organizacja Techniczna)  
Warszawa, Poland. Vol. 5, no. 1, January 1959

Monthly list of East European Accession (EEAI) LC, Vol. 8, no. 7, July 1959

Uncl.

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CIA-RDP86-00513R000823910002-6

.. K. BUDILOV, L. I. DORMAN, V. I. IVANOV, Ye. V. KOLMEYETS, L. Y. MIROSHNIKOVA

Small Flares and the Propagation of Solar Cosmic Rays in Interplanetary Space.

report submitted for the 8th Intl. Conf. on Cosmic Rays (IUPAP), Jaipur India,  
2-14 Dec 1963

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CIA-RDP86-00513R000823910002-6"

~~KOLMOGOROV, A., mashinist ekskavatora.~~

Work without idling. Mast.ugl.5 nc.4:12-13 Ap '56. (MIRA 9:7)  
(Kuznetsk Basin--Strip mining)

KOLMOGOROV, A. N. i KHinchin A. A.

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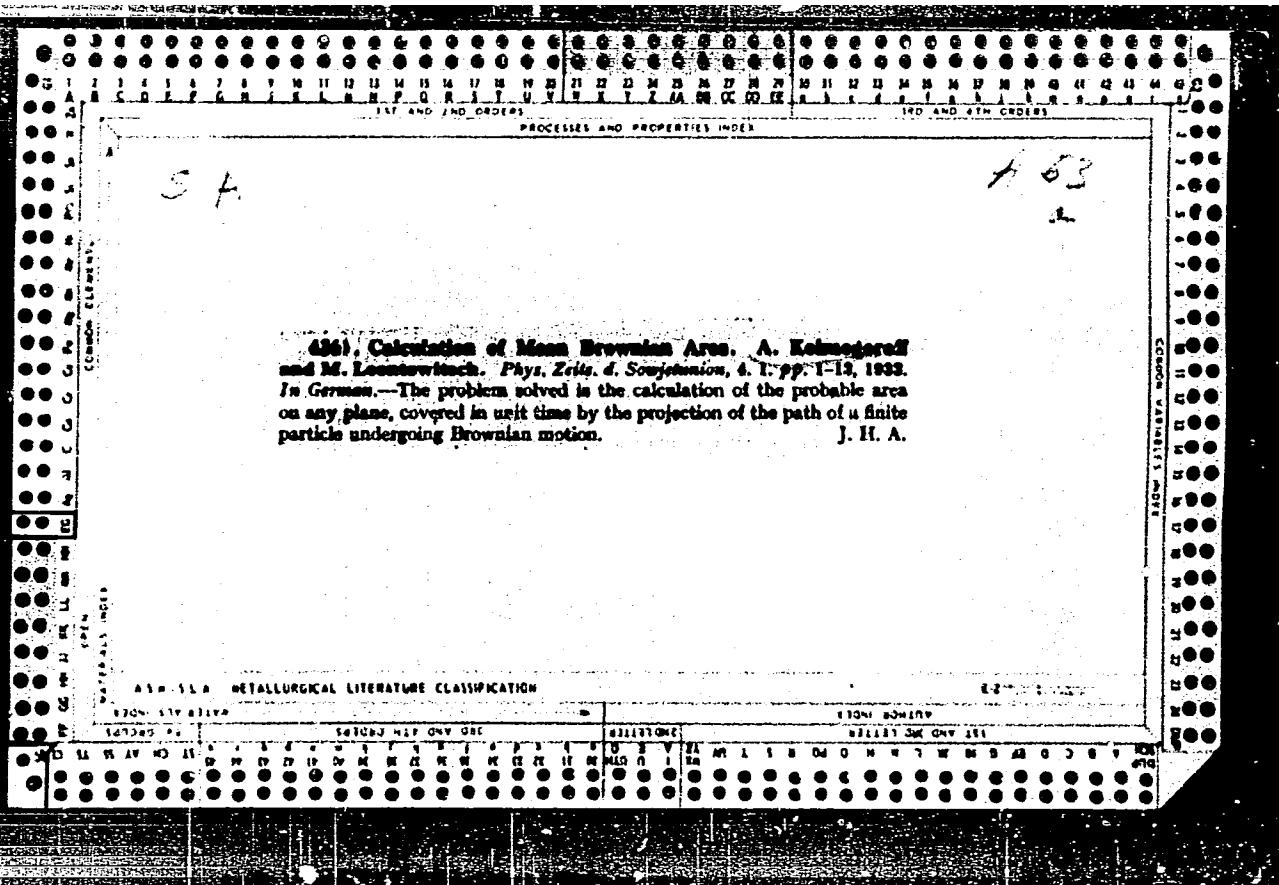
So: Mathematics in the USSR, 1917-1947

edited by Kurosh, A. G.

Markushevich, A. I.

Rashevskiy, P. K.

Moscow-Leningrad, 1948



KOLMOGOROV, A. N.

- O printsipe tertium non datur. Matem. SB., 32 (1925), 646-667.  
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Teoriya i praktika v matematike. Front nauki i tekhniki, 5 (1936), 39-12.  
Sovremennaya matematika. SB. Statey po fil. Matem. M., Uchpedgiz (1936),  
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N'yuton i sovremennoye matematicheskoye myshleniye. V kn. "moskovskiy universitet-pamyati Isaaka N'yutona". M., Izd. un-ta (1946), 47-52.  
Rol' russkoy nauki v razvitiu teorii veroyatnostey. M, uchen, zap, un-ta, 91 (1947),  
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Zur topologisch-gruppentheoretischen begründung der geometrie. Gott. Nachr., 2 (1930),  
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Zur begründung der projektiven geometrie. Ann of math, 33 (1932), 275-276.  
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KOLMOGOROV, A. N.

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Markushevich, A. I.,  
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Moscow-Leningrad, 1948

KOLMOGOROV, A.N. (con't)

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KOLMOGOROV, A. N.

Krivyye v gil'bentovskom prostranstve, invariantnyye po otnosheniyu k odnoparametricheskoy gruppe dvizheniy. Dan, 26 (1940), 6-9.

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Sur la loi des grands nombres. C.R. Acad. Sci., 135 (1927), 919-921.

Ueber die summen durch den zu fall bestimmter unabhangiger grossen. Math. Ann., 99 (1928), 309-319.

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Matematika. BSE, T. 38 (1938), 359-401.

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N'yuton i sovremennoye matematicheskoye myshleniye. V SB. Mockovskiy Universitet - pamyati n'yutona. M., Izd. un-ta (1946), 27-42.

Rol' russkoy nauki v razvitiu teorii veroyatnostey. M., Uchen. zap un-ta, 91 (1947), 53-64.

SO: Mathematics in the USSR, 1917-1947

Edited by Kurosh, A.G.,

Markusevich, A.I.,

Rashevskiy, P.K.

Moscow-Leningrad, 1948

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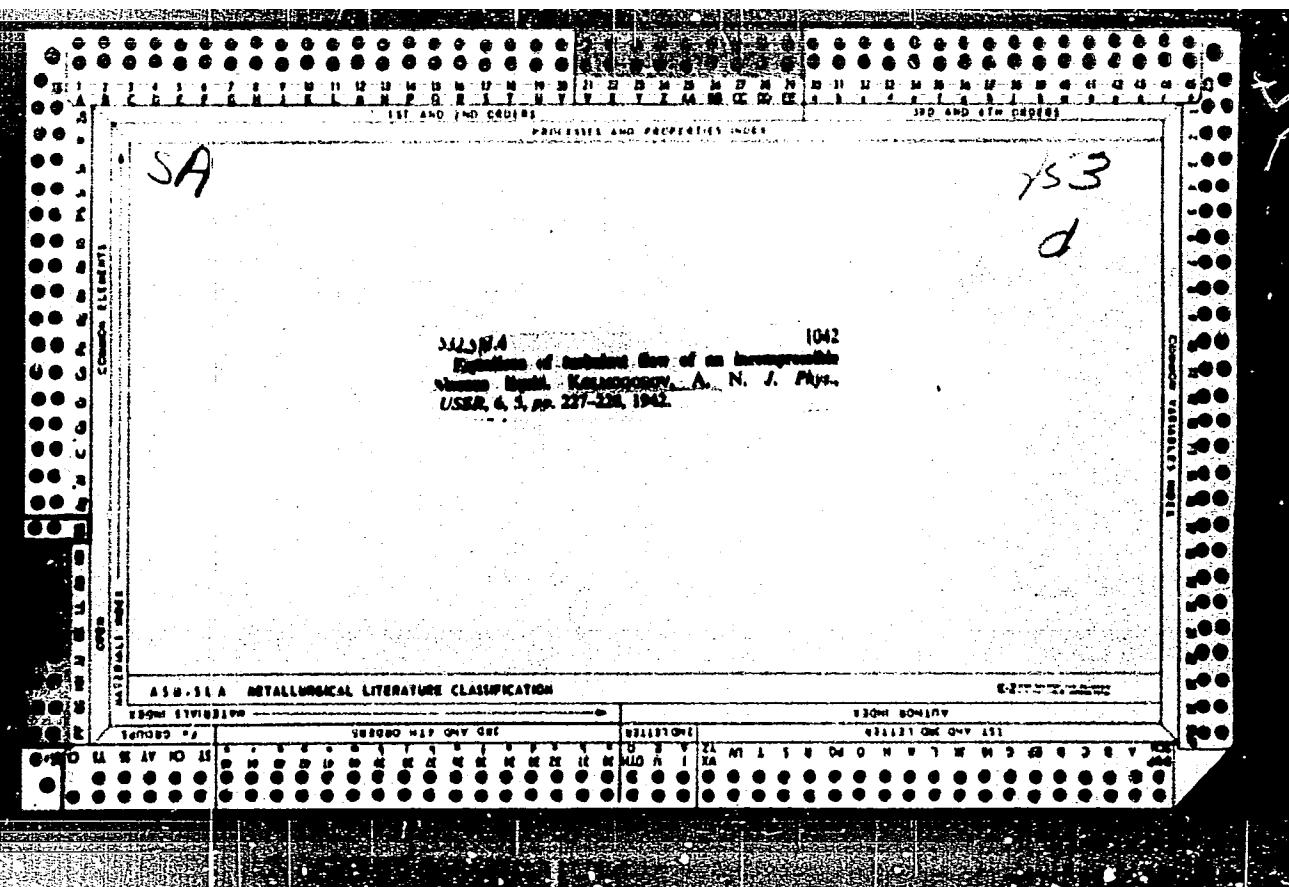
CIA-RDP86-00513R000823910002-6

KOLMOGOROV, A. N.

"The Local Structure of Turbulence in an Incompressible Viscous Liquid,"  
Doklady AN USSR, Vol XXX, no 4, 1941.

APPROVED FOR RELEASE: 09/18/2001

CIA-RDP86-00513R000823910002-6"



KOLOMOGOROV, A. N., Academician

Mbr., Dept. Physico-Mathematical Sci., Acad. Sci. (1944)

"Fundamental Problems in the field of Mathematics and Science," Vest. Ak. Nauk SSSR,  
No. 11-12, 1944

BR-52059019

Kolmogorov, A. N. On the proof of the method of least squares. Izv. Matem. Nauk (N.S.) 1(11), no. 1, 57-1046. (Russia)

The author criticizes general textbook expositions of the theory of least squares. Two counter-they fail to indicate that the Gaussian error law seriously overestimates the reliability of the results derived from small samples and derive their main results by a cumbersome set of calculations rather than by the lucid methods of vector algebra. The paper is written to show how this condition can be corrected.

Vector methods are illustrated as follows. Let us assume a linear relation  $y = \sum_{j=1}^n a_j x_j$ , where  $a_j$  are unknown constants. We make  $N$  experimental observations on the  $y$  and  $x_j$ 's, thus determining a set of  $n+1$  vectors in Euclidean  $N$ -space, with components  $y, x_1, x_2, \dots, x_n$ . We suppose that the rank of the matrix  $(x_1, x_2, \dots, x_n)$  is  $n$ . The linear vector equation  $y = \sum_{j=1}^n a_j x_j$  cannot in general be satisfied; we seek, therefore, the most reason-

able set of values  $a_j$  to approximate the  $a_j$ . Write  $\eta = y + \epsilon$ ,  $\xi_j = x_j - a_j$ , and  $\epsilon = y - \eta$ . It is clear that  $\eta^*$  belongs to the linear subspace  $L$  spanned by the  $x_j$ . Denoting scalar products by  $[\cdot, \cdot]$ , we see that the condition  $[\eta, \xi_j] = \text{minimum}$  is equivalent to the condition that  $\eta^*$  is the orthogonal projection of  $y$  on  $L$ , whence  $[\epsilon, \xi_j] = 0$  follows. A further immediate consequence is that  $\sum_{j=1}^n [\xi_j, \xi_j] a_j = [\xi_j, \eta]$ ,  $j=1, \dots, n$ . These are the normal equations for the  $a_j$ , and have a solution since determinant  $[\xi_j, \xi_j] \neq 0$ .

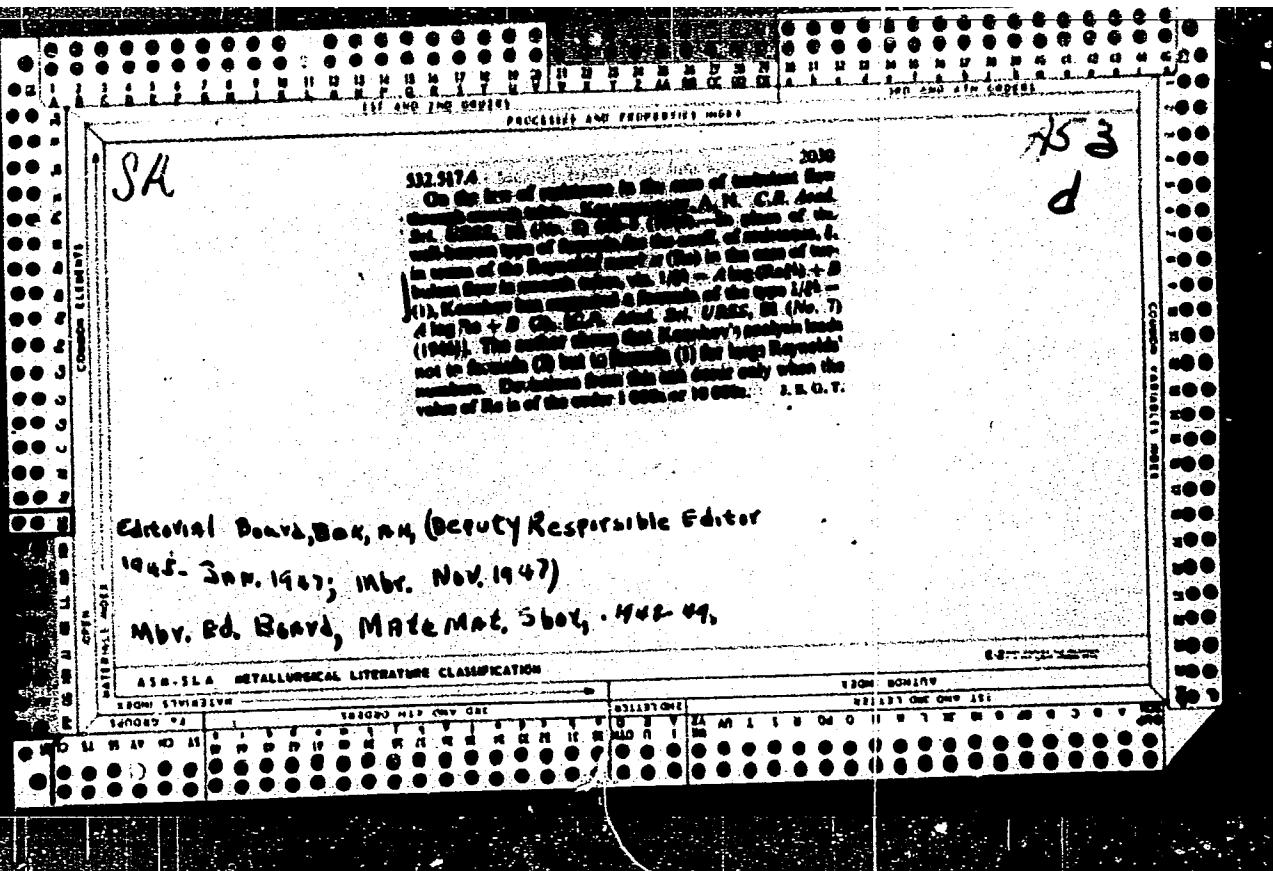
Next, define a set of vectors  $u_i \in L$  by  $[u_i, \xi_j] = \delta_{ij}$  (Kronecker symbols) and write  $[u_i, u_j] = q_{ij}$ . Then  $a_j = a_i + [\Delta u_i]$ . If we suppose that the components  $\Delta_i$  of  $\Delta$  are random variables with mean value zero and finite variances independent of  $u_i$  and with  $M$  the appropriate mean value operator, we find that  $M a_i = a_i$  and  $M(a_i - a_j)(a_i - a_j) = q_{ii} s^2$ . Similarly, one derives  $M \epsilon = 0$  and  $M \epsilon \epsilon = (N-n)s^2$ .

The  $\chi^2$ -distribution and Student's distribution are derived and there are brief discussions of confidence limits and of the significance of the dispersion matrix  $q_{ij}$ .

A. I. Brown (Alexandria, Va.)

Mathematical Reviews,

Vol. 8 No. 6



KOLMOGOROV, A. N.

Kolmogorov, A. N., Petryv, A. A., and Smirnov, Yu. M.

A formula of Gauss in the theory of the method of least squares. Izvestiya Akad. Nauk SSSR Ser. Mat. 11, 361-366 (1947). (Russian)

In articles 39-40 of Gauss's *Theoria Combinationis Observationum Erroribus Minimis Obnoxiae* there occurs the inequality  $\rho\rho/\pi \leq \sum(a\alpha+b\beta+c\gamma+\dots)^2 < \pi$ . Gauss failed to notice that this inequality can be sharpened. The purpose of the paper is to show that  $\rho\rho/\pi \leq \sum(a\alpha+b\beta+c\gamma+\dots)^2 \leq \rho$  and that this latter inequality cannot be improved.

W. R. Mann (Corvallis, Ore.)

Source: Mathematical Reviews,

Vol 9

No. 7

KOLMOGOROV, A. N.

Kolmogoroff, A. N., and Dmitriev, N. A. Branching sto-  
chastic procesaes. [J. R. (Doklady) Akad. Nauk SSSR (N.S.) 56, 5-8 (1947).]

Suppose that objects are divided into  $n$  types. There are transitions in which each object goes into one or more objects of each of the  $n$  types, in accordance with some probability law. The transitions are independent of each other and of past transitions. If  $\alpha(t)$  is the vector whose  $k$ th component is the number of objects of type  $k$  at time  $t$ , the  $\alpha$  process is then a Markov process, and the standard theory of Markov processes can be applied, but it is necessary to use methods adapted to this special case. When  $n = 1$ , the process becomes the birth process studied by many authors [see, for example, R. A. Fisher, The Genetical Theory of Natural Selection, Oxford University Press, 1930]. The authors find a functional equation and a differential equation for the generating function of the  $\alpha(t)$  distribution, and show how simply the differential equation can be used to find the transition probabilities of a simple birth process examined by Arley [On the Theory of Stochastic Processes and their Application to the Theory of Cosmic Radiation, Copenhagen thesis, 1943; these Rev. 7, 209].

J. L. Doob (Urbana, Ill.).

Source: Mathematical Reviews, 1948, Vol. 9, No. 1

*CONFIDENTIAL*

Kolmogorov, A. N., and Savostyanov, B. A. The calculation of final probabilities for branching random processes. Trudy Akad. Nauk SSSR (N.S.) 56, 783-786 (1960).

Soit  $P_{\text{fin}}(t) = P(T_1 = \alpha_1 T_2 + \dots + \alpha_n T_n | t)$  la probabilité qu'une particule du type  $T_1$  donne, après  $K$  générations,  $n$  particules du type  $T_2, \dots, T_n$ ,  $\alpha_i$  particules du type  $T_i$ . La fonction génératrice  $F_k(t; z) = \sum_{\alpha} P_{\text{fin}}(t) x_1^{\alpha_1} \dots x_n^{\alpha_n}$ ,  $F_k(t; x) = f_k(x)$ , est donnée par

$$F_k(t+1; x) = f_k(F_k(t; x), \dots, F_k(t; x)).$$

Introduisant si d le faut un type fictif dont les particules demeurent invariantes, que  $f_d(0, \dots, 0) = 0$ , l'ensemble  $T_1, \dots, T_n, \dots, T_d$  est dit fermé si les particules qui en peuvent produire que des particules du même groupe, on suppose le système total indécomposable dans les fermés. Un groupe est dit final si (a) il est fermé, et chacune de ses particules produit une particule

exactement, (c) il ne contient aucun sous-groupe ayant la propriété (a). Si à l'intérieur d'un groupe final les transformations constituent un cas particulièrement simple des chaînes de Markoff. Soit  $v(\varphi_1, \dots, \varphi_n) = \sum_{\alpha} f_{\alpha} u_1^{\alpha_1} \dots u_n^{\alpha_n}$  la fonction génératrice des  $q^{\alpha} = P(T_k = \beta_1 v_1 + \dots + \beta_n v_n | \infty)$ , en décomposant le système total en groupes finals  $V_m = \{T_m, \dots, T_{m_s}\}$ ,  $r=1, \dots, s$ , et en types  $T_m, \dots, T_{m_s}$  n'appartenant pas à des groupes finals; si on écrit  $T_m$  au lieu de  $T_k$ , on écrira  $\varphi_m$  au lieu de  $\varphi_k$  et  $f_m$  au lieu de  $f_k$ . Théorème 1. Les relations

$$\begin{aligned} \varphi_m &= f_m(\varphi_1, \dots, \varphi_s), & m &= 1, \dots, n, \\ \varphi_m &= u_r, & 0 \leq r < 1 + m - 1, & m > n, \\ && k &= 1, \dots, n, \end{aligned}$$

déterminent univoquement les valeurs des  $\varphi_k$  pour les  $\varphi_m$  données. On montre, par exemple, étudié en détail, comment le cas de l'continuité peut se ramener au cas discret.

M. Feller (New York, N. Y.).

Mathematical Reviews. 1948, Vol. 9, No. 3

*Spur*

Soviet

Theory of Functions of Real Variables

and Equations of Mathematical Physics

Introduction to the Theory of Sets and the Theory of Functions

Part One - Aleksandrov, P. S., Vedenie

o teorii mnozhestv i funktsij. Cetvertaja

časina. Teoriya funkciy

General Theory of Sets and Functions

Costin, L. I.

Teoriia Lit. M. L. Leningrad, 1946.

411 pp.

This volume is the first of a two-volume treatise dealing with the foundations of modern-day mathematical analysis, designed for students of mathematics in Soviet universities and pedagogical institutes. The thesis is advanced that the broadest sections of set theory, topology, space, community, and integral should find a place in the curriculum for students of higher mathematics. The study of these concepts, only faintly mentioned or passed over in view of the development of mathematics in the past half century, is an anchorage point one (written by Aleksandrov) deals with topics related essentially to cardinal numbers and continuity. Part two (written by Kostin) is devoted to the theory of integration and its applications. A third volume (written by Vilenkin) deals with dynamical systems, and the fourth (written by Vilenkin under the editorship of the authors) deals with functional analysis. It furnishes proofs and arguments in favor of the authors' thesis. It requires some knowledge in the way of previous training

P.S. Aleksandrov. Card 1 of 2

12 NOV 9

The reader's part covers the descriptive theory of real functions. Part II is concerned with the number of methods of analysis and is divided into two parts. All of the basic concepts and methods are illustrated by well-chosen examples. A number of the topics handled will indicate the importance of the book.

Chapter I: basic notions about sets; main types of sets, ordered sets, cardinal equivalence classes, the Schröder-Bernstein theorem. Chapter II: definition of the real number system in terms of Dedekind cuts in the rational number system; elementary properties of sets of real numbers. Chapter III: basic properties of well-ordered sets; the axiom of choice; the well-ordering theorem (Bernardi's third proof); standard theorems on and classification of infinite cardinal numbers. Chapter IV: elementary topology of the line and plane. All the usual concepts are introduced and all standard theorems are proved. Chapter V: continuous real-valued functions on the line; functions of bounded variation; the Weierstrass approximation theorem for closed intervals (Bernstein's proof is given); there is one of the few proofs in the book not admitting generalization to the most general case of derivatives. Chapter VI: definition of metric spaces; open and closed sets; Borel sets; subspaces; closure and interior; dense sets; connectedness; compactness; homeomorphisms; mappings of metric spaces; several topological separation axioms; Urysohn's imbedding theorem. Chapter VII: compact and complete metric spaces; Banach spaces. In conclusion, one may observe that a book is called "classic" if essentially accessible to students, it might well have a deep and broad influence on mathematical education.

P.S. Aleksandrov Card 2 of 2

KOLMOGOROV, A. N.

Kolmogorov, A. N. A remark on the polynomials of P. L.  
Chebyshev deviating the least from a given function.  
Uspehi Matem. Nauk (N.S.) 3, no. 1(23), 216-221 (1948).  
(Russian)

From a necessary and sufficient conditions for the uniqueness  
of the "polynomial in  $f_1(x), f_2(x) - c_1f_1(x) - \dots$   
 $- c_nf_n(x)$ , deviating the least from a given function  $F(x)$  of  
a real variable  $x$ , we extended to a complex variable.

E. Kogbetliantz (New York, N. Y.).

Source: Mathematical Reviews,

Vol. 10, No. 1

*Kolmogorov, D.V.*

Kolmogorov, A. N. Obituary [Evgenii Evgen'evich Slutskii].  
Uspeni. Matem. Nauk. (N.S.) 3, no. 4(29), 143-151  
(I-plate) (1948). (Russian)

Slutskii, N. Obituary: Evgenii Evgen'evich Slutskii.  
1880-1948. Izdat. Akad. Nauk SSSR, 1948.

Source: Mathematical Reviews, Vol. 10 No. 3



| There is a section on antimodular distributions & Levy's theorem  
| that all limiting laws in Levy's class of distributions are  
| **antimodular**.

Chapters VII-IX comprise a third section. Subheads  
are:

| Chapter VII: Lattice distributions. Includes a proof of the  
| central limit theorem for densities of discrete distributions, and  
| some related topics.

Chapter VIII: Local limit theorems for the case of lattice  
distributions.

This book is an invaluable compendium of the most  
important work on the subject, and is the more striking  
because of the general lack of systematic and rigorous texts  
in probability theory.

Source: Mathematical Reviews.

Vol. 11 No. 10

C.A.

2

"(Isometric selection" of crystals. A. N. Kolmogorov. Doklady Akad. Nauk S.S.R. R. 60, 601-4 (1949).—Implicit math. derivations concerning the problem of a selection of crystals growing on the plane boundary of a crystallizing mass; article material of photographs furnished from expts. # of G. G. Lomonosov was used. The crystals grew between 2 parallel glass plates, as in the expts. of Shmelev and Lomonosov (ibid. #627, 61). Graphic figures were projected in gradually increasing sizes, to represent, as 2-dimensional models, the gradually growing crystals. The initial orientation of these figures was at random, corresponding to a statistical no. distribution (Lomonosov, ibid. 60, 177 (1947)). The calc. starts from the probability function for the growth of an elongated crystal (needle) to a given length, as a function of the no. of directions of a max. rate of growth. The 3-dimensional analog is implicitly discussed. W. E.

Kolmogorov, A. N.

Kolmogorov, A. N. The solution of a problem in the theory  
of probability connected with the notion of the mecha-  
nism of the formation of strata

ДАН. 65, 721-726 (1947). [RUSSIAN]

It is assumed that strata are formed by periods of sedi-  
mentation followed by erosion. If  $h_n$  is the height of  
a stratum at the end of the  $n$ th period,  $t_n = h_n - h_{n-1}$ ,  
 $n = 1, 2, \dots$ , are assumed to be mutually independent ran-  
dom variables with a common density function  $\varphi(x)$ , and a  
positive expectation. Let  $t_n^{(0)} = \delta_1 + \dots + \delta_n$ . By the strong  
law of large numbers,  $\lim_{n \rightarrow \infty} t_n^{(0)} = +\infty$  and  $\varphi_* = \min \{t_n^{(0)}\}$   
is therefore determinate. If  $\varphi_* > 0$ , the deposit from the  $n$ th  
period finally disappears, and if  $\varphi_* > 0$ , the residue ap-  
proaches  $\varphi_*$ . Let  $f(x)$  be the density of distribution of  $\varphi_*$   
and let  $\rho = \Pr(\varphi_* > 0) = f_0(0)/f(x)$ . It is shown that  $f(x)$  is  
the unique solution of the integral equation

$$f(x) = \rho \varphi(x) + \int_x^{\infty} g(x-y) f(y) dy,$$

and that it can be obtained by a simple iterative procedure.  
The condition of convergence is

$$\int_0^{\infty} g(x-y) dy < 1$$

Source: Mathematical Reviews, Vol. 10, No. 10



Kolmogorov, A. N. A local limit theorem.  
Izvestiya Akad. Nauk SSSR

1938, 7, 300-304. (Russian)

The author considers a Markov chain with step transitions from the initial state  $x_0$  to the first  $n$  states in the first  $t$  transitions from the initial state. The vector with components  $(\mu(t))_n$  is called the first  $t$ -step transition probability vector. If  $t$  is large enough, it is possible to pass from  $\mu(t)$  to  $\mu(\infty)$ , i.e., to the central limit theorem. This is done by using the covariance matrix of the random variable  $\mu(t)$ . The covariance matrix is defined by the formula  $E[\mu(t)\mu(t)^T]$ . The central limit theorem is obtained if the covariance matrix has a definite positive value. It is shown that the covariance matrix of the random variable  $\mu(t)$  is uniformly bounded for all  $t$  and does not depend on the initial state  $x_0$ .

Assume that (A) the covariance matrix of the random variable  $\mu(t)$  is uniformly bounded for all  $t$ ; (B) the covariance matrix of the random variable  $\mu(t)$  is uniformly bounded for all  $t$  and the random variable  $\mu(t)$  converges in distribution to a 1-dimensional standard normal distribution which is denoted by  $\varphi(x)$ . Then the following local limit theorem is proved:

$E[\mu(t)] = \varphi(0) + o(1).$

$E[\mu(t)] = \varphi(0) + O(1).$

Uniformly for bounded  $t$ . Here  $\varphi(x)$  is the normal form of the central limit theorem.

Finally, it is shown how these results are related to hypotheses (A) and (B).

It is shown that hypotheses (A) and (B) are not satisfied if a finite procedure involving examination of the positions of the nonzero elements of the transition matrix of the process.

Sources: Mathematical Reviews, 1940, Vol. 1, No. 2

Kolmogorov, A. N. et al.

PA 5747100

On the Local Structure of Turbulence in Fluids

Jun 49

"The Breaking-Up of Drops in a Turbulent Stream,"  
Acad A. N. Kolmogorov, 4 pp.

"Dok Ak Nauk SSSR" Vol LVI, No 5

Author and A. N. Obukhov present a theory of the local structure of turbulent pulsations, but believe that the idea of a hard lower facet with the dimensions of the drop and not undergoing further breaking up under assigned conditions should be further developed and experiments should be conducted on the time relation of the distribution of dimensions. Submitted 1A Aug 49.

50/497100

KOLMOGOROV, A. N. (ACAD)

PA 156T91

USSR/Physics - Conductivity, Thermal Mar/Apr 50  
Agriculture - Soil Science

"Problem of Determining the Coefficient of Temperature Conductivity of Soils," Acad A. N.  
Kolmogorov, 2 pp

"Iz Ak Nauk SSSR, Ser Geograf i Geofiz" Vol XIV,  
No 2

Proposes method of calculating "temperature" conductivity of soil from temperatures at two depths at four moments of time. This improved method eliminates several defects in method proposed by M. A. Kaganov and A. F. Chudnovskiy.  
Submitted 14 Dec 49

156T91

1. SEVAST'YANOVA, B. A.; KOLMOGOROV, A. N.
2. USSR (600)
4. Science
7. Introduction to theory of probabilities and mathematics statistics. Per. a angl  
A. S. Monina i A. A. Petrova. Pod Red. B. A. Sevast'yanova. Arley, N.; Bukh, K. R.  
(Authors) Fredial. A. N. Kolmogorova. Moskva. Izd. Inostr. Lit. 1951.
9. Monthly List of Russian Accessions, Library of Congress, January, 1953. Unclassified.

KOLMOGOROV, A.N.

Gnyegyenko, B.V., és Kolmogorov, A.N. Független valószínűségi változók összegeinek határeloszlásai. [ Limit distributions for sums of independent random variables.] Akadémiai Kiadó, Budapest, 1951. 256 pp. 32.00 florints.

Translation of Gnedenko and Kolmogorov, Predel'nye raspredeleniya dlya summ nezavisimyh sluchainyh veličin [ Gostehizdat, Moscow-Leningrad, 1949; these Rev. 12, 839 ]. The translation is by I. Földes.

SO: Mathematical Review, Vol. 14, No. 3, March 1953, pp. 233-340.

A. N. Tikhonov, *On the construction of the foundations of the theory of measures*, i.e., Učen. Matem. Nauk. SSSR, no. 11(35), 111-153 (1950). (Russian)

The author sketches a method whereby the original definition of measure given by Lusin can be replaced so that the countably additive measure  $m$  on certain abstract sets  $U$  will be any set, and let  $\mathcal{E}$  be a family of subsets  $A$  of  $U$ , denoted as elementary sets. Let  $m(A)$  be a nonnegative function defined for all  $A \in \mathcal{E}$ . Let  $\lambda$  be any number of  $\mathbb{R}$ . If there exists a countable subfamily  $\{A_i\}_{i=1}^{\infty}$  of  $\mathcal{E}$  such that  $A \subseteq \bigcup_{i=1}^{\infty} A_i$ , let the set-function  $\lambda(A)$  be defined as  $\sum_{i=1}^{\infty} m(A_i)$ ; the infimum being taken over all countable families  $\{A_i\}_{i=1}^{\infty}$  such that  $A \subseteq \bigcup_{i=1}^{\infty} A_i$ . If no such family  $\{A_i\}_{i=1}^{\infty}$  exists, let  $\lambda(A) = +\infty$ . A subset  $B$  of  $U$  is said to be Lebesgue measurable if, for all  $A \in \mathcal{E}$ , the equality  $\lambda(A \cap B) = \lambda(A) - \lambda(B \setminus A)$  obtains. This author states that  $\lambda$  is a "rather arbitrary" outer measure, and that measurability in the sense of Lebesgue is equivalent to the usual measurability in the sense of Carathéodory. [Proofs of these assertions are "certainly supplied."]

Let  $\lambda$ , when defined only on the family  $\mathcal{E}$ , be Lebesgue measurable sets, be denoted by the symbol  $L$ . It is next stated that a set-function  $\mu$  defined on a family  $\mathcal{G}$  of subsets of  $U$  (such that  $\emptyset \subseteq \mu(A) \leq \lambda(A) + \epsilon$ ) can be obtained by the construction described above if and only if the following conditions are satisfied: (1) the family of sets  $\mathcal{G}$  contains a largest set and is closed under the formation of countable unions and intersections; (2)  $\mu$  is countably additive; (3) if  $A \in \mathcal{E}$ ,  $\mu(A) = 0$ , and  $B \subset A$ , then  $\mu(B) = 0$ . Finally, the author notes that, under the above construction, all elementary measurable and  $m(A) = \mu(A)$  for all elementary sets.

If the following conditions are satisfied: (4) if  $A \in \mathcal{G}$  is a countable subfamily of  $\mathcal{E}$  such that  $m(A) = \sum m(A_i)$  and (5) given  $A$  and  $A' \in \mathcal{G}$  and  $\epsilon > 0$ , there exist countable subfamilies  $\{A_i\}$  and  $\{A'_j\}$  of  $\mathcal{E}$  such that  $A \cap A' \subseteq \bigcup_{i=1}^{\infty} A_i \cup \bigcup_{j=1}^{\infty} A'_j$  and  $\sum m(A_i) + \sum m(A'_j) + \epsilon > m(A \cap A')$ , then the odd feature that, in some simple case, there are no Lebesgue measurable sets. For example, let  $U$  be any infinite set, and let  $\{x_1, x_2, \dots, x_n, \dots\}$  be a countably infinite subset of  $U$ . Let  $\mathcal{E}$  be the family of all sets consisting of a single point. Let  $m(x_i) = \alpha_i$ , where  $i = 1, 2, \dots, n, \dots$  and no other  $A$  of  $U$  is Lebesgue measurable. On the other hand, if  $i = 0$ , then  $\lambda(\emptyset) = 0$  and all subsets of  $U$  are Lebesgue measurable. [R. Henley (Seattle, Wash.)]

CRCV, A.N.

F. N. DALEY, A. N. TURBINER

Vestn. Mat. Mat. Mekh. Mat. 14, 303-326 (1950). (Russian)

The purpose of this expository article is to stimulate interest in the theory of statistical estimation, and specifically on the theories of ~~of statistics~~ and ~~and statistical~~ estimation. Writing apparently for a reader with more training in practical statistics than in pure mathematics, the author discusses some of the elementary properties of estimators and contains some of their elementary properties. He discusses in great (and even numerical) detail some examples involving binomial and normal distributions (the former in the language of the theory of quality control). Although according to the author the paper presumes to do no more

than to demonstrate by example that the theory of estimation is not fully pitched in the abstract, the author does not seem to have any real desire to do so. The paper is divided into two parts. The first part is concerned with the theory of unbiased estimation of a sufficient statistic [Ann. Math. Statistics 18, 34-43 (1946); these Rev. 7, 48]. The second part is concerned with the theory of generalized form, and these generalizations are later applied to simplify the proofs of some of the reviewer's results on symmetric unbiased estimates [Ann. Math. Statistics 17, 34-43 (1946); these Rev. 7, 463]. P. R. Halmos.

Source: Mathematical Reviews, Vol. 12, No. 2.

KOLMOGOROV, A. N.

Kolmogorov, A. N. Generalization of Poisson's formula to  
the case of a sample from a finite set. Uspich Matem.  
Nauk (N.S.) 5, no. 3(43), 131-134 (1951). (Russian)

distribution defined by the probabilities

$$\Pr(X = k) = \frac{m!}{k!(m-k)!} \lambda^k e^{-\lambda},$$

where  $\omega = -\lambda + \log(1-\lambda)$ ,  $\lambda = m/N$ . *M. L. Ladevèze*

Sources: Mathematical Reviews,

Vol. 12, No. 7

KOLMOGOROV, A.N.

188T62

## USER/Mathematics - Mathematician

May/Jun 51

"Ivan Georgiyevich Petrovsky, on the Occasion of His 50th Birthday," A. N. Kolmogorov

"Uspekh Matemat Nauk" Vol VI, No 3 (43), pp 160-164  
 Member of the mathematical school founded by D. F. Yegorov in Moscow. Elected in 1946 as an active member of Acad Sci USSR, where he was at first deputy director of the Math Inst and later academician-Secretary of the Physicomath Dept. In May 1951 nominated rector of Moscow U, where he had been a student, candidate, and finally professor. Edits the most important Soviet mathematical periodical "Matemat Sbornik," and also "Trudy Matemat

188T62

USSR/Mathematics - Mathematician  
(Contd)

May/Jun 51

Inst, Ak Nauk SSSR." Awarded 3 orders of Workers' Red Banner. Lists 36 works.

188T62

KOLMOGOROV, A.N.

188T64

USSR/Mathematics - Probability May/Jun 51

"Review of G. P. Boyev's Book "Theory of Probability," A. N. Kolmogorov

"Uspekhi Matemat Nauk" Vol VI, № 3 (43), pp 175-181

Subject book published 1950 by State Tech Press for 9.45 rubles; 15,000 copies. Authorized by the Ministry of Higher Educ of USSR as textbook for higher institutions of learning. Review is favorable. Reviewer states that scientific literature on the theory of probability in the USSR is not very abundant.

188T64

KOLMOGOROV, A. N.

191782

USSR/Mathematics - Functionals

Jul/Aug 51

"Works of I. M. Gel'fand on the Algebraic Problems of Functional Analysis," A. N. Kolmogorov

"Uspekhi Matemat Nauk" Vol VI, No 4 (44), pp 184-186

Subject work won a Stalin prize. Gel'fand succeeded in touching a basic and most fruitful line of work on reconstructing all of functional analysis in the algebraic direction. Modern mathematics uses extensively the general geometric and algebraic methods by considering, on the one hand, the most diverse systems of objects (functions, lines, etc.) as a certain geometric entity--namely, space--and, on

USSR/Mathematics - Functionals

(Contd)

Jul/Aug 51

the other hand, diverse systems of objects with the operations on them as algebraic forms --namely, groups, rings, or flds. These represent 2 directions to follow in mathematics.

191782

KOLMOGOROV, A. N.

191T84

## USSR/Mathematics - Statistics, Mathematics

Jul/Aug 51

"The Works of N. V. Smirnov on the Study of the Properties of Variational Series and on the Non-parametric Problems of Mathematical Statistics,"  
A. N. Kolmogorov, A. Y. Khinchin

"Uspekhi Matemat Nauk" Vol VI, No 4 (44), pp 190-192

Until recently in math statistics one was limited almost exclusively to problems of detg the parameters. For example, earlier it was assumed that the distribution function  $F(x)$  possesses the usual gaussian form and the usual parameters  $\alpha$

191T84

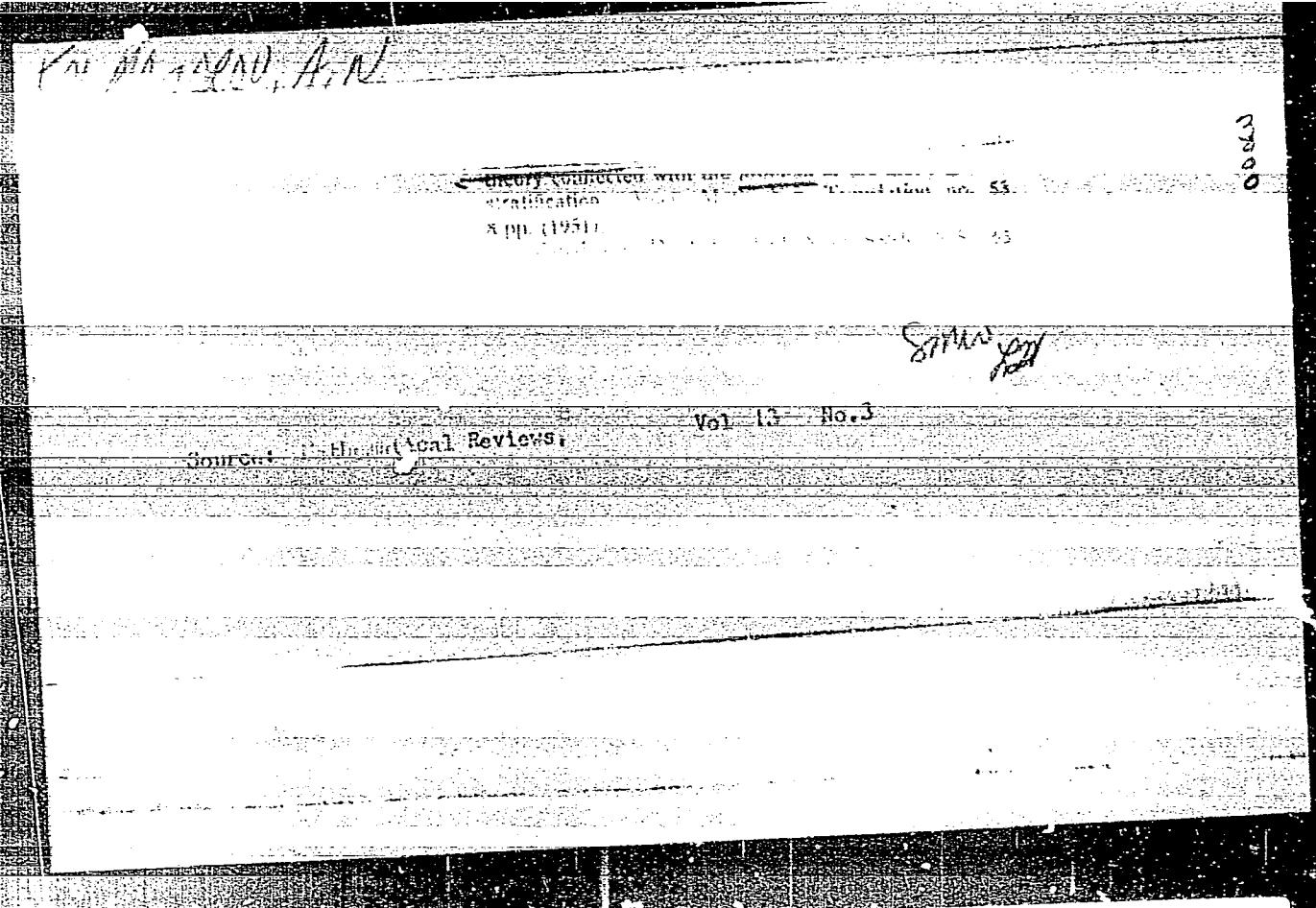
USSR/Mathematics - Statistics, Mathematical (Contd) Jul/Aug 51

(shift) and sigma (spread) are evaluated from the observed quantities  $x_1, x_2, \dots, x_n$ . Often such an approach is artificial in problems. However, Smirnov considered all possible types of distribution functions and terms.

191T84

"APPROVED FOR RELEASE: 09/18/2001

CIA-RDP86-00513R000823910002-6



APPROVED FOR RELEASE: 09/18/2001

CIA-RDP86-00513R000823910002-6"

KOLMOGOROV, A. N.

Kolmogorov, A. N. On the differentiability of the transition probabilities in stationary Markov processes with a denumerable number of states. Moskov. Gos. Univ. Učenye Zapiski 148, Matematika 4, 53-59 (1951). (Russian)

The author considers Markov chains with infinitely many states and stationary transition probabilities. Let  $[p_{ij}(t)]$  be the matrix of transition probabilities for time  $t$ . It is assumed that  $\lim_{t \rightarrow 0} p_{ii}(t) = 1$ . The reviewer has shown [Trans. Amer. Math. Soc. 52, 37-64 (1942); these Rev. 4, 17] that then  $p_{ij}'(0) = a_{ij}$  exists for  $j \neq i$ , and for  $j = i$  if  $a_{ii} > -\infty$ . The author gives new proof of these facts, proving also that  $a_{ij}$  exists and is finite in all cases. He gives simple examples of pathological cases in which, for a single value of  $i$ ,  $a_{ii} = -\infty$ , and in which every  $a_{ij}$  is finite but, for a single value of  $i$ ,  $\sum_j a_{ij} \neq 0$ . In the latter example, the backward differential equations for the transition probabilities are no longer valid. See also the pathological examples given by Lévy [Ann. Sci. École Norm. Sup. (3) 68, 327-381 (1951); these Rev. 13, 959]. J. L. Doob.

SOI REV. 474, NO. 3, P0233-210 (unclassified)  
March 1953

KOLMOGOROV, A. N.

Mathematical Reviews  
Vol. 15 No. 4  
Apr. 1954  
Analysis

8-24-54

LL

\*Aleksandrov, P. Sz. és Kolmogorov, A. N. Bevezetés  
a halmazelméletbe és a függvénytanba. Első rész.  
[Introduction to the theory of sets and the theory of  
functions. Part one.] - Aleksandrov, P. Sz. Bevezetés  
a halmazok és függvények általános elméletébe. [In-  
troduction to the general theory of sets and functions.]  
Akadémiai Kiadó, Budapest, 1952. 276 pp. 45 Ft.  
Translation by Gy. Bizám of Aleksandrov's Vvedenie v  
obščuyu teoriyu množestv i funkciy [Gostehizdat, Moscow-  
Leningrad, 1948; these Rev. 12, 682].

DELONE, B. N.; KUROSH, A. G.; KOLMOGOROV, A. N.; MARKOV, A. A.; GEIFOND, A. O.;  
MEYMAN, N. N.; VILENKN, N. Ya.

Algebra

Development of algebra. Usp.nat.nauk 7 No. 3, 1952.

9. Monthly List of Russian Accessions, Library of Congress, November 1951, Uncl.<sup>2</sup>

KOLMOGOROV, A. N.

PA 242T78

USSR/Mathematics - Prize Winners

Sep/Oct 52

"Mathematical Life in the USSR: Works Winning a Stalin Prize," A. N. Kolmogorov

"Usp Matemat Nauk" Vol 7, No 5(51), pp 234-7

Dr of Phys-Math Sci S. N. Mergelyan awarded prize in 1951 for works on constructive theory of functions, main results of which were expounded in his article "Uniform Approximations of Functions of a Complex Variable" (ibid., 7, No 2 (1952)). S. M. Nikol'skiy's prize-winning works during 1949-1951 represent the culmination of 10 years' work in his single program of approximations of functions following the investigations of S. N. Bernshteyn.

242T78

KOLMOGOROV, A.N.

USSR/Physics - Hydrodynamics

1 May 52

"Problem Concerning Resistance and Velocity Profile During Turbulent Flow in Pipes," Acad A. N. Kolmogorov

"Dok Ak Nauk SSSR" Vol LXXXIV, No 1, pp 29, 30

Discusses subject formulas of P. K. Konakov, A. D. Al'tshul', and Nikuradze. States that G. A. Gurzhienko's assertion concerning the small influence of a wall on indications of micro-setting is fully founded by expts. Submitted 19 Mar 52.

224T93

KOLMOGOROV, A. N.

Mathematical Reviews  
May 1954  
Analysis

(2) ✓ Kolmogoroff, A. A. Stationary sequences in Hilbert spaces. Trabajos Estadistica 4, 55-73, 243-270 (1953).  
(Spanish)  
Translated from Byull. Moskov. Gos. Univ. Matematika 2 (1941); these Rev. 5, 101.

10-7-54

LL

"APPROVED FOR RELEASE: 09/18/2001

CIA-RDP86-00513R000823910002-6

FIDMAN, B.A.; KOLMOGOROV, A.N., akademik.

Velocity of a water current at a sudden increase of depth. Izv. AM SSSR  
Otd. tekh. nauk no. 4:512-522 Ap '53.  
(MLRA 6:8)  
(Hydrodynamics)

APPROVED FOR RELEASE: 09/18/2001

CIA-RDP86-00513R000823910002-6"

KOLMOGOROV, A.N.

Oct 53

USSR/Mathematics - Probability

"Certain Works of Recent Years in the Field of  
Limit Theorems of Probability Theory," A.N.  
Kolmogorov

Vest Mos Univ, Ser Fizkomat i Vest Nauk, No 7,  
pp 19-38

Mentions his and B.V. Gnedenko's Predel'nyye  
Raspredeleniya dlya Sumn Nezavisimykh Sluchay-  
nykh Velichin (Limit Distributions for Sums of  
Independent Chance Quantities), 1949. Refers to  
related works of R.L. Dobrushin (Izv AN SSSR,  
17, 1953); Yu. V. Prokhorov (Uspehi Mat Nauk, 8,  
17, 1953).

273T91

No 3, 1953; DAN SSSR, 83, 1952); D.G. Meyzler,  
O.S. Parasyuk, and Ye. L. Ryacheva (DAN SSSR,  
60, 1948; Ukr Mat Zhur, 9-20, 1949); Ye.L. Ryacheva  
(Trudy Inst Mat i Mekh AN UzbSSR, No 10, part 1,  
1953); Yu. V. Linnik and N.A. Sapogov (Izv AN  
SSSR, 13, 1949); S. Kh. Sirazhdinov (DAN SSSR,  
84, 1952).

KOLMOGOROV, A. N. Acad.

"Certain Questions of the Qualitative Theory of Dynamic Systems with an Integral Invariant," report given at the All-University Scientific Conference "Lomonosov Lectures", Vest. Mosk. Un., No.8, 1953

Translation U-7895, 1 Mar 56

KOLMOGOROV, A.N.

Some work of recent years on boundary theorems in the theory of probabilities. Vest. Mosk. un. 8 no.10:29-38 0 '53. (MLRA 7:1)  
(Chains (Mathematics))

GEL'FAND, I.M.; GRAEV, M.I.; KOLMOGOROV, A.N., akademik.

Unitary representations of a real unimodular group (principal non-degenerate series). Izv. AN SSSR 17 no. 3:189-248 My-Je '53. (MLRA 6:5)

1. Akademiya Nauk SSSR (for Kolmogorov).

DOBROUSHIN, R.L.; KOLMOGOROV, A.N., akademik.

Boundary theorems for a Markoff chain of two forms. Izv. AN SSSR Ser. mat.  
17 no.4:291-330 Jl-Aug '53.  
(MLR 6:7)  
(Probabilities)

PUGACHEV, V.S.; KOLMOGOROV, A.N., akademik.

General correlation theory of random functions. Izv.AN SSSR Ser.mat. 17 no.5:  
401-420 8-0 '53. (MLRA 6:10)

1. Akademiya nauk SSSR (for Kolmogorov).

(Correlation (Statistics))

KOLMOGOROV, A. N.

USSR/Mathematics - Markov Chains

1 May 53

"Ergodic Principle for Nonhomogeneous Markov Chains," T.A. Sarymsakov, Active Member, Acad Sci Uzbek SSR, Central Asiatic State U

DAN SSSR, Vol 90, No 1, pp 25-28

Considers a simple nonhomogeneous and discrete Markov chain with uniquely possible and disjoint states  $w_1, w_2, \dots, w_s$ , which is completely detd by the assignment of a sequence of stochastic matrices (V.I. Romanovskiy, Acta Math. 66, 174 (1935); A.N. Kolmogorov, Usp Mat Nauk, No 5 (1938); S.N. Bernshteyn, Teoriya Veroyatnostey, Theory of Probabilities, 4th ed, 1948).  $A_k = //p_{ij}(k)//$  ( $k=1, 2, \dots$ ;  $i, j=1, 2, \dots, s$ ), where  $p_{ij}(k)$  is the conditional probability that state  $w_i$  remaining at moment  $t_k$  will pass over to state  $w_j$  at moment  $t_{k+1}$  (i.e., in one step). Presented 22 Dec 52.

259T70

ARESHKIN, G.Ya.; KOLMOGOROV, A.N., akademik.

Congruence relations in distributive structures with zero elements. Dokl.  
AN SSSR 90 no.4:485-486 Je '53. (MLRA 6:5)

1. Akademiya Nauk SSSR (for Kolmogorov).

(Congruences (Geometry))

MIKELADZE, Sh.Ye.; KOLMOGOROV, A.N., akademik.

Theory of the construction of interpolation formulas. Dokl. AN SSSR 90 no.  
4:503-506 Je '53. (MIR 6:5)

1. Akademiya Nauk SSSR (for Kolmogorov). 2. Tbilisskiy matematicheskiy  
institut Akademii nauk Gruzinskoy SSR (for Mikeladze). (Interpolation)

BARI, N.K.; KOLMOGOROV, A.N., akademik.

Generalization of inequalities of S.N. Bernstein and A.A. Markov. Dokl.  
AN SSSR 90 №.5:701-702 Je '53. (MLRA 6:5)

1. Akademiya Nauk SSSR (for Keldysh). (Inequalities (Mathematics))

YAGLOM, A.M.; PINSKER, M.S.; KOLMOGOROV, A.N., akademik.

Random processes with fixed increments of the n-th order. Dokl. AM SSSR  
90 no.5:731-734 Je '53. (MLRA 6:5)

1. Akademiya Nauk SSSR (for Kolmogorov). (Probabilities)

KHAPLANOV, M.G.; KOLMOGOROV, A.N., akademik.

Spectral theory of matrixes in an analytical space. Dokl. AN ~~SSSR~~ 90  
no.6:969-972 Je '53. (MLB 6:6)

1. Rostovskiy gosudarstvennyy universitet im. V.M.Molotova (for Khaplanov).
2. Akademiya nauk SSSR (for Kolmogorov).  
(Matrixes) (Spaces, Generalized)

KRASNOSEL'SKIY, M.A.; POLOVITSKIY, A.I.; KOLMOGOROV, A.N., akademik.

Variational methods in the problem for points of bifurcation. Dokl. AN  
SSSR 91 no.1:19-22 J1 '53. (MLRA 6:6)

1. Akademiya nauk SSSR (for Kolmogorov).  
(Spaces, Generalized) (Calculus of variations)

SOBOLEV, V.I.; KOLMOGOROV, A.N., akademik.

Semiordered measures of sets, measurable functions, and certain abstract  
integrals. Dokl. AN SSSR 91 no.1:23-26 J1 '53. (MLRA 6:6)

1. Voronezhskiy gosudarstvennyy universitet. 2. Akademiya nauk SSSR (for  
Kolmogorov). (Integrals) (Aggregates)

DYNKIN, Ye.B.; KOLMOGOROV, A.N., akademik.

Construction of primitive cycles in compact Lie groups. Dokl. AN SSSR 91  
no.2:201-204 Jl '53. (MLRA 6:6)

1. Akademiya nauk SSSR (for Kolmogorov). (Topology) (Groups, Theory of)

KOLMOGOROV, A.N., akademik; MOKRISHCHEV, K.K.

Solvability of construction problems of the second order in the Lobachevski plane, with the aid of a hypercompass or compass and oricompass. Dokl. AN SSSR 91 no.3:453-456 Jl '53. (MLRA 6:7)

1. Rostovskiy gosudarstvennyy universitet imeni V.M. Molotova (for Mokrishchev). 2. Akademiya nauk SSSR (for Kolmogorov). (Geometry, Plane)

USPENSKIY, V.A.; KOLMOGOROV, A.N., akademik.

Gödel's theorem and the theory of algorithms. Dokl. AN SSSR 91 no.4:  
737-740 Ag '53. (MIRA 6:8)

1. Akademiya nauk SSSR (for Kolmogorov).  
(Aggregates) (Algorithm)

VINOGRAD, R.E.; KOLMOGOROV, A.N., akademik.

Instability of characteristic indexes of proper systems. Dokl.An SSSR 91  
no.5:999-1002 Ag '53. (MLRA 6:8)

1. Akademiya nauk SSSR (for Kolmogorov).

(Matrixes)

DYNKIN, E.H.; KOLMOGOROV, A.N., akademik.

Homological characteristics of homomorphisms in compact Lie groups. Dokl.  
AN SSSR 91 no.5:1007-1009 Ag '53.  
(MLRA 6:8)

1. Akademiya nauk SSSR (for Kolmogorov).

(Groups, Continuous)

RODNYANSKIY, A.M.; KOLMOGOROV, A.M., akademik.

Integral representations of the degree of mapping. Dokl.AN SSSR 91 no.5:  
1019-1021 Ag '53. (MIR 6:8)

1. Akademiya nauk SSSR (for Kolmogorov). 2. Moskovskiy khimiko-tehnologicheskiy institut myasnoy promyshlennosti. (Surfaces, Representation of)

KHARAZOV, F.F.; KOLMOGOROV, A.N., akademik.

One class of linear equations with symmetrizable operators. Dokl.AN SSSR 91  
no.5:1023-1026 Ag '53.  
(MLRA 6:8)

1. Akademiya nauk SSSR (for Kolmogorov). 2. Tbilisskiy matematicheskiy  
institut im. A.Razmadze Akademii nauk Gruz.SSR.  
(Differential equations)

AL'BER, S.I.; KOLMOGOROV, A.N., akademik.

Homologs of a space of surfaces and their applications to variational calculus.  
Dokl. AN SSSR 91 no.6:1237-1240 Ag '59. (MLRA 6:8)

1. Akademiya nauk SSSR (for Kolmogorov). 2. Tomskiy gosudarstvennyy universitet im. V.V.Kuybysheva. (Topology) (Calculus of variations)

BEREZANSKIY, Yu.M.; KOLMOGOROV, A.N., akademik.

Hypercomplex systems constructed on Sturm-Liouville equation on the semiaxis.  
Dokl. AN SSSR 91 no.6:1245-1248 Ag '53. (MLRA 6:8)

1. Akademiya nauk SSSR (for Kolmogorov). 2. Institut matematiki Akademii  
nauk Ukrainskoy SSR. (Topology) (Differential equations)

BERMAN, D.L.; KOLMOGOROV, A.N., akademik.

Approximation of periodic functions by linear, trigonometric polynomial operations. Dokl. AN SSSR 91 no.6:1249-1252 Ag '53. (MLRA 6:8)

1. Akademiya nauk SSSR (for Kolmogorov). (Functions, Periodic) (Polynomials)

GANZBURG, I.M.; KOLMOGOROV, A.N., akademik.

Approximation of functions with a given module of continuity, by P.L.Cheby-  
shev's sums. Dokl. AN SSSR 91 no.6:1253-1256 Ag '53. (MLB 6:8)

1. Akademiya nauk SSSR (for Kolmogorov). 2. Dnepropetrovskiy gosudarstvennyy  
universitet. (Functions)

SMIRNOV, Yu.; KOIMOGOROV, A.N., akademik.

Completeness of uniform spaces and spaces of proximity. Dokl.AN SSSR 91  
no.6:1281-1284 Ag '53. (MLN 6:8)

I. Akademiya nauk SSSR (for Kolmogorov). (Topology) (Spaces, Generalized)

KHARAZOV, D.F.; KOLMOGOROV, A.N., akademik.

Theory of symmetrizable operators, depending polynomially on the parameter.  
Dokl.AN SSSR 91 no.6:1285-1287 Ag '53. (MLRA 6:8)

1. Akademiya nauk SSSR (for Kolmogorov). 2. Tbilisskiy matematicheskiy  
institut im. A.Razmadze Akademii nauk Gruzinskoy SSR.  
(Functional analysis)

SHILOV, G.Ye.; KOLMOGOROV, A.N., akademik.

Criterion of compactness in a uniform space of functions. Dokl. AN SSSR  
92 no. 1:11-12 8 '53. (MLRA 6:8)

1. Akademiya nauk SSSR (for Kolmogorov).

(Spaces, Generalized)

Khavinson, S.Ya.; KOLMOGOROV, A.N., akademik.

Certain non-linear extremal problems for bounded analytic functions. Dokl. AN  
SSSR 92 no.2:243-245 S '53. (MLRA 6:9)

1. Akademiya nauk SSSR (for Kolmogorov). 2. Yeletskiy gosudarstvennyy uchitel'-  
skiy institut (for Khavinson). (Functions, Analytic)

FRANKL', F.I.; KOLMOGOROV, A.N., akademik.

Theory of movement in suspended depositions. Dokl.AN SSSR 92 no.2:247-250  
S '53. (MIRA 6:9)

1. Akademiya nauk SSSR (for Kolmogorov). 2. Kirgizskiy gosudarstvennyy uni-  
versitet (for Frankl'). (Fluid mechanics)  
(Sedimentation and deposition)

MIKELADZE, Sh.Ye.; KOLMOGOROV, A.N., akademik.

Expansion of finite differences from functions in differences of its derivative. Dokl.AN SSSR 92 no.3:479-482 S '53. (MLRA 6:9)

1. Akademiya nauk SSSR (for Kolmogorov). 2. Matematicheskiy institut Akademii nauk Gruzinskoy SSR (for Mikeladze). (Difference equations)

ORLOV, S.A.; KOLMOGOROV, A.N., akademik.

Defect index for linear differential operators. Dokl. AN SSSR 92 no.3:483-  
486 S '53. (MLR 6:9)

1. Akademiya nauk SSSR (for Kolmogorov).  
(Operators (Mathematics)) (Differential equations, Linear)

FADDEYEV, D.K.; KOLMOGOROV, A.N., akademik.

One theory of the theory of homologies in groups. Dokl. AN SSSR 92 no.4:703-  
705 O '53. (MLRA 6:9)

1. Akademiya nauk SSSR (for Kolmogorov). 2. Leningradskiy gosudarstvennyy  
universitet im. A.A. Zhdanova (for Kolmogorov). (Groups, Theory of)

BEREZANSKIY, Yu.M.; KOLMOGOROV, A.N., akademik.

Proper function analysis of partial difference equations. Dokl.AN SSSR 93  
no.1:5-8 N '53. (MLRA 6:10)

1. Akademiya nauk SSSR (for Kolmogorov). 2. Institut matematiki Akademii  
nauk Ukrainskoy SSR (for Berezanskiy). (Difference equations)

MONIN, A.S.; OBUKHOV, A.M.; KOLMOGOROV, A.N., akademik.

Dimensionless characteristics of turbulence in the surface layer of the atmosphere. Dokl.AN SSSR 93 no.2:257-260 N '53. (MLRA 6:10)

1. Akademiya nauk SSSR (for Kolmogorov). 2. Geofizicheskiy institut Akademii nauk SSSR (for Monin and Obukhov). (Atmosphere)

BEREZANSKIY, Yu.M.; KOLOMGOROV, A.N., akademik.

Unique determination of the Schrödinger equation by its spectral function.  
Dokl. AN SSSR 93 no. 4: 591-594 D '53. (MLRA 6:11)

1. Akademiya nauk SSSR (for Kolmogorov). 2. Institut matematiki Akademii  
nauk Ukrainskoy SSR (for Berezanskiy).  
(Geometry, Differential--Projective)

KOLMOGOROV, A.N.

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U.S.S.R. Kolmogorov, A. N. On dynamical systems with an integral invariant on the torus. Doklady Akad. Nauk SSSR (N.S.) 93, 763-766 (1953). (Russian)

The author considers a dynamical system defined on a 2-dimensional torus  $T^2$  by the system of differential equations

$$(1) \quad \frac{dx}{dt} = A(x, y), \quad \frac{dy}{dt} = B(x, y),$$

and possessing an invariant integral  $I(g) = \iint_{T^2} U(x, y) dx dy$ , where  $A, B$  and  $U$  are univalued, analytic periodic functions of  $x$  and  $y$  with period  $2\pi$ . Here  $x$  and  $y$  are real coordinates mod  $2\pi$ ,  $A^2 + B^2 > 0$ ,  $U > 0$  on the whole of  $T^2$ . It is then known [Nemyckii and Stepanov, Qualitative theory of differential equations, 2nd. ed., Gostchizdat, Moscow-Leningrad, 1949; for a review of the 1st ed. see these Rev. 10, 612] that there exists an analytic transformation of coordinates which transforms the system (1) into the system

$$(2) \quad \frac{dx}{dt} = \frac{1}{F(x, y)}, \quad \frac{dy}{dt} = \frac{\gamma}{F(x, y)}$$

2/3 KOLMOGOROV, A. I.

with an integral invariant  $I(g) = \iint_{\mathbb{R}^2} F(x, y) dx dy$  where  $\gamma$  is a constant.

The following theorem is asserted. Theorem 1: If there exist constants  $c > 0$  and  $k > 0$  such that for all positive integers  $m$  and  $n$ :

$$(1) \quad |x - ny| \geq ck^n,$$

then there exists an analytic transformation of coordinates which transforms the system (2) into the system

$$(3) \quad \frac{du}{dt} = \lambda_1, \quad \frac{dv}{dt} = \lambda_2,$$

where  $\lambda_1, \lambda_2$  are constants and  $\lambda_2 = \gamma \lambda_1$  and with the integral invariant  $I(g) = \mathcal{K} \iint_{\mathbb{R}^2} dudv$ . Condition (1) is fulfilled for every  $\gamma$  except for a set of Lebesgue measure zero ( $c$  and  $k$  depend on  $\gamma$ ). It follows that system (1) has a pure point spectrum with analytic proper functions.

For those irrational numbers which do satisfy (1) the author states: Theorem 2. Each of the following conditions is possible for a suitable choice of  $\gamma$  and  $F(x, y)$ : The system (2) can be transformed into (3) by (I) an infinitely differentiable but not analytic transformation, (II) a  $k$ -differentiable

3/3 Kolmogorov, A.N.

able but not  $(k+1)$ -differentiable transformation; (III) an everywhere discontinuous transformation; and (IV) the system (2) cannot be transformed into (3) at all. In (I), (II) and (III) the original system (1) has a pure point spectrum but the proper functions are respectively not analytic, not  $k+1$  differentiable and everywhere discontinuous. The conjecture is made that in (IV) the spectrum is necessarily continuous but only a considerably weaker result is proved. In all statements related to Theorem 2 the notions of analyticity, differentiability, etc. are interpreted modulo sets of Lebesgue measure zero. The method of obtaining the system (3) from (2) is obtained and discussed.

*P. N. Dauker (London).*

KREYN, M.G.; KOLMOGOROV, A.N., akademik.

Certain cases of effective determination of the density of a heterogenous string by its spectral function. Dokl. AN SSSR 93 no. 4:617-620 D '53.  
(MIRA 6:11)

1. Akademiya nauk SSSR (for Kolmogorov).  
(Vibration) (Mathematical physics)

KOIMOGOROV, A.N., akademik; SOROKIN, I.S., redaktor; GUBER, A., tekhnicheskiy redaktor.

[The profession of a mathematician] O professii matematika, Izd. 2-e, dop. Moskva, Gos. izd-vo "Sovetskaiia nauka," 1954. 29 p.  
(Mathematics as a profession) (MIRA 7:11)

KOLMOGOROV, A.N.

QA331.K73

## TREASURE ISLAND BOOK REVIEW

AID 777 - M

KOLMOGOROV, A. N., FOMIN, S. V.

ELEMENTY TEORII FUNKTSIY I FUNKTIONALNOGO ANALIZA. Vypusk I  
 METRICHESKIYE I NORMIROVANNYYE PROSTORANSTVA (Elements of the theory  
 of functions and functional analysis. Issue I: Metrical and  
 normed spaces). Izdatel'stvo Moskovskogo Universiteta, 1954.  
 153 p.

This textbook was written by A. N. Kolmogoroff, one of the outstanding Russian Scientist mathematicians, assisted by Professor S. V. Fomin, for students of graduate schools in the mathematical faculty of Russian universities.

The first chapter of this text is devoted to a brief exposition of some basic ideas of the theory of sets in which modern functional analysis is needed. A more extensive text on this subject of the introduction to the general theory of sets and functions has been written by another outstanding Russian mathematician, P. S. Alexandroff. This text is recommended by Kolmogoroff as an additional text to his first chapter (p. 5). For more extensive study of the whole field of the theory of sets, the fundamental book on this subject, the Grundzüge der Mengenlehre, written by F. Hausdorff,

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KOLMOGOROV APPROVED FOR RELEASE: 09/18/2001 CIA-RDP86-00513R000823910002-6"

FOMIN, S. V., Elementy teorii . . . AID 777 - M

was translated from the German into Russian in 1936. [The first German edition of this book was reprinted in the U.S.A. in 1949].

The second, third and fourth Chapters on metrical spaces, linear normed spaces, and linear operational equations respectively, are written on the basis of the modern theory of functional analysis, in whose creation Kolmogoroff took part by writing many articles. The most famous of his articles include:

I. Über die analytischen Methoden der Wahrscheinlichkeitsrechnung.  
Math. Annalen, 104 (1931) 415-458.

II. Sulla forma generale di un processo stocastico omogeneo. (Un problema di Bruno de Finetti). Atti Accad. naz. Lincei, Rend., (6) 15 (1932) 805-808, 866-869.

III. Zur Normierbarkeit eines allgemeinen topologischen linearen Raumes. Studia Math., 5 (1934) 29-33.

A very important supplement called "Generalized functions" was added to the third chapter - Linear normed spaces - .

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KOLMOGOROV, A. N., FOMIN, S. V., Elementy teorii . . . AID 777 - M

In this supplement the method of determining of generalized functions, constructed by the Russian scientist S. L. Sobolev was used. This method was published in several articles in Russia in 1935-1936 (p. 129).

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KOLMOGOROV A.M.

LYAPUNOV, A.M.; SRETENSKIY, L.N., otvetstvennyy redaktor; KOLMOGOROV, A.M., akademik; SMIRNOV, V.I., akademik; SUBBOTIN, M.F.; ISHLINSKIY, M.YU.; MIGIRENSKO, G.S., kandidat fizicheskikh-matematicheskikh nauk; PETROVICH, V.V., kandidat fizicheskikh-matematicheskikh nauk; GERMOGENOV, A.V., redaktor; ALEXEYEVA, T.V., tekhnicheskiy redaktor.

[Collected works] Sobranie sochinenii. Moskva, Izd-vo Akademii nauk SSSR. Vol. 1. 1954. 446 p.  
(MLRA 7:11)

1. Chlen-korrespondent Akademii nauk SSSR (for Sretenskiy and Subbotin) 2. Deystvitel'nyy chlen Akademii nauk SSSR (for Ishlinsky)  
(Lyapunov, Aleksandr Mikhailovich, 1857-1918) (Mathematics)

KUMLD-OROV

Kolmogoroff, Andrej: und Prokhorov, G. A.: Fundamentals und Grenzwertungssätze. Bericht Nr. 1-11 W die Tagung Wahrscheinlichkeitstheorie und mathematische Statistik, 1955, Berlin, 1956. Institut für Statistik und Wahrscheinlichkeitstheorie der Universität Wien.

An amalgam of two expository lectures. Of particular interest is the treatment of probability measures on abstract sets which goes from the most abstract definition to applications to specific probability distributions.

translation [Akadémiai Kiadó, Budapest, 1951; these Rev. 14, 294] are incorporated. Appendix I by J. L. Doob contains further remarks on some of the topics of Ch. I. The translator has also corrected minor misprints and annotated the text. He wishes to call attention to the following error: The footnote on p. 16 should read "in A but not in B."

KOLMOGOROV, A. N.

USSR/Physics - Suspension Pumps

FD-767

Card 1/2 : Pub 129-4/24

Author : Kolmogorov, A. N.

Title : M. A. Velikanov's new variant of his gravitational theory of motion  
of suspension pumpsPeriodical : Vest. Mosk. un., Ser. Fizikomat, i yest. nauk, Vol 9, No 2, 41-45  
Mar 1954

Abstract : The author claims that the new variant (M. A. Velikanov, "Motion of suspension pumps," Vest. Mosk. un., No. 8, 1953) of Velikanov's "gravitational theory" of the transfer of suspended particles by a turbulent current, first proposed by Velikanov in 1944, leads to conclusions so paradoxical and so roughly inconsistent with daily experience that the theory's defective basis has become particularly evident. Velikanov's fundamental idea of the role of the "energy of suspension", which is essentially correct, is here analyzed for any errors and also for the possibility of its more correct development. The author refers to a related work of G. I. Barenblatt ("Motion of suspended particles in a turbulent current," Prikl. mat. i mekh., 17, No. 3, 261-272, 1953).

(no institution)

Submitted: December 16, 1953

KOLMOGOROV, A. N.

USSR/Mathematics - Mechanics

Card 1/1 : Pub. 22 - 4/49

Authors : Kolmogorov, A. N., Academician

Title : On conservation of conditionally periodic movements at a small change  
of Hamilton's function

Periodical : Dok. AN SSSR 98/4, 527-530, Oct. 1, 1954

Abstract : A theorem, quite important for mechanics, is proved. The theorem  
states that a s-parametric system of conditionally periodic movements,  
such as  $q_\alpha = \lambda\alpha t + q_\alpha^{(0)}$ ;  $p_\alpha = 0$ , under certain conditions outlined  
in the theorem, can not vanish as a result of small changes of Hamil-  
ton's function governing the movements. Three references (1936-1953).

Institution : ...

Submitted : ...

KOLMOGOROV, A.N., akad.; MIMYTSKIY, V.V., prof., otv.red.

[Program in the theory of probability; for the Mechanics-Mathematics Faculty. Major: mathematics] Programma po teorii veroyatnosti dlia mekhaniko-matematicheskogo fakul'teta. Spetsial'nost' - matematika. 1956. 1 p. (MIRA 11:3)

1. Moscow. Universitet.  
(Probabilities)

ALEKSANDROV, A.D., redaktor; KOLMOGOROV, A.N., akademik, redaktor; LAVRENT'YEV, M.A., akademik, redaktor; BYKOV, A.Z., redaktor izdatel'stva; POLIVANOVA, Ye.B., tekhnicheskiy redaktor; ZELENKOVA, Ye.V., tekhnicheskiy redaktor

[Mathematics, its content, methods, and significance] Matematika, ee soderzhanie, metody i znachenie. Moskva. Vol.1. 1956. 294 p. Vol.2. 1956. 395 p. Vol.3. 1956. 336 p. (MIRA 9:12)

1. Akademiya nauk SSSR. Matematicheskiy institut. 2. Chlen-korrespondent AN SSSR (for Aleksandrov)  
(Mathematics)

LYAPUNOV, Aleksandr Mikhaylovich, akademik; SRETENSKIY, L.N., redakter;  
KOLMOGOROV, A.N., akademik, redakter; SMIRNOV, V.I., akademik,  
redakter; SUBBOTIN, M.F., redakter; ISHLINSKIY, A.Yu., redakter;  
MIGIREVSKII, G.S., kandidat fiz.-mat. nauk, redaktor; PETKEVICH,  
V.V., kandidat fiz.-mat. nauk, redaktor; KIRNARSKAYA, A.A., tekhnicheskiy  
redaktor.

[Collected works] Sobranie sochinenii. Moskva, Izd-vo Akademii  
nauk SSSR. Vol.2. 1956. 472 p. (MLRA 9:6)

1. Chlen-korrespondent AN SSSR (for Sretenskiy, Subbotin).
2. Deystvitel'nyy chlen AN USSR (for Ishlinskiy)  
(Dynamics) (Differential equations)